

Course Topics

A) Basics of MHD

- i) MHD equations, content
- ii) Freezing-in Law, Alfven's Theorem
- iii) Energy and momentum relations, magnetic tension
- iv) Virial Theorem, Stellar Collapse

B) MHD Dynamics I

- i) MHD Waves, Fredericks Diagram
- ii) Reduced MHD, Model Structure, Drift Wave Models
- iii) Deriving MHD Models
- iv) Nonlinear Alfven waves, basics of collisionless shocks

C) Non-ideal MHD I

- i) Local Reconnection: Sweet–Parker Model
- ii) Magnetic Helicity — a measure of self-linkage
- iii) Global: Prandtl–Batchelor Theorem, Flux Expulsion

D) Stability I — Ideal

- i) MHD Energy Principle — formulation
- ii) Examples
 - a) Rayleigh–Benard
 - b) Rayleigh–Taylor
 - c) Interchange, line-tying
- iii) Magnetic instabilities
 - a) Sausage mode and hydro-analogue
 - b) Kink, Kruskal–Shafranov Criterion
 - c) MRI

E) Wave Interactions

- i) Wave Adiabatic Theory

- ii) 3-wave interactions, Manly–Rowe relations
- iii) Wave kinetics, non-local interactions, wave cascades
- iv) Decay instability of Alfvén wave

F) Basics of MHD Turbulence

- i) Navier–Stokes Turbulence — a very brief review
- ii) MHD turbulence — basic ideas, Alfvén effect
- iii) Kraichnan-Iroshnikov and Goldreich-Sridhar Scalings, critical balance

G) Non-ideal MHD II

- i) Stochastic magnetic fields, transport
- ii) Magnetic Helicity II, Selective Decay, Taylor Relaxation
- iii) Basics of dynamo theory
- iv) Mean field electrodynamics — an introduction

H) Stability II — Resistive

- i) Basic ideas of resonances, resistive modes
- ii) Fast, slow resistive interchange
- iii) Tearing, magnetic island formation

I) Tokamak MHD

- i) Nonlinear tearing modes, Rutherford Theory, Neoclassical Tearing
- ii) Ballooning modes, beta limits
- iii) ELM dynamics